

Maxima 5.10.0 <http://maxima.sourceforge.net>  
Using Lisp GNU Common Lisp (GCL) GCL 2.6.7 (aka GCL)  
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Dedicated to the memory of William Schelter.  
This is a development version of Maxima. The function bug\_report()  
provides bug reporting information.

(%i1) K[1]:g(t,y)

(%o1) g(t, y)

(%i2) A:taylor(g(t+h[t],y+h[y]),[h[t],h[y]],0,4)

$$\begin{aligned}
& \text{( \%o2 ) } g(t, y) + \left( \left( \frac{d}{dh_t} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_t + \left( \frac{d}{dh_y} g(t, h_y + y) \Big|_{h_y=0} \right) h_y \right) + \\
& \frac{\left( \frac{d^2}{dh_t^2} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_t^2 + 2 \left( \frac{d^2}{dh_t dh_y} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_y h_t + \left( \frac{d^2}{dh_y^2} g(t, h_y + y) \Big|_{h_y=0} \right) h_y^2}{2} + \\
& \frac{\left( \frac{d^3}{dh_t^3} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_t^3 + 3 \left( \frac{d^3}{dh_t^2 dh_y} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_y h_t^2 + 3 \left( \frac{d^3}{dh_t dh_y^2} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_y^2 h_t + \left( \frac{d^3}{dh_y^3} g(t, h_y + y) \Big|_{h_y=0} \right) h_y^3}{6} + \\
& \frac{\left( \frac{d^4}{dh_t^4} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_t^4 + 4 \left( \frac{d^4}{dh_t^3 dh_y} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_y h_t^3 + 6 \left( \frac{d^4}{dh_t^2 dh_y^2} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_y^2 h_t^2 + 4 \left( \frac{d^4}{dh_t dh_y^3} g(h_t + t, h_y + y) \Big|_{h_t=0} \right) h_y^3 h_t + \left( \frac{d^4}{dh_y^4} g(t, h_y + y) \Big|_{h_y=0} \right) h_y^4}{24}
\end{aligned}$$

(%i3) h[t]=mu[21]\*h

(%o3) h\_t = mu\_21 h

(%i4) h[y]=mu[21]\*h\*K[1]

(%o4) h\_y = mu\_21 h g(t, y)

(%i5) K[2]:A,%o3,%o4,ratexpand

$$\begin{aligned}
& \text{( \%o5 ) } \frac{\mu_{21}^4 h^4 \left( \frac{d^4}{d(\mu_{21}^4 h^4)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right)}{24} + \\
& \frac{\mu_{21}^4 h^4 g(t, y) \left( \frac{d^4}{d(\mu_{21}^3 h^3) d(\mu_{21} h g(t, y))} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right)}{6} + \\
& \frac{\mu_{21}^3 h^3 \left( \frac{d^3}{d(\mu_{21}^3 h^3)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right)}{6} + \\
& \frac{\mu_{21}^4 h^4 g(t, y)^2 \left( \frac{d^4}{d(\mu_{21}^2 h^2) d(\mu_{21}^2 h^2 g(t, y)^2)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right)}{4} + \\
& \frac{\mu_{21}^3 h^3 g(t, y) \left( \frac{d^3}{d(\mu_{21}^2 h^2) d(\mu_{21} h g(t, y))} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right)}{2} + \\
& \frac{\mu_{21}^2 h^2 \left( \frac{d^2}{d(\mu_{21}^2 h^2)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right)}{2} + \\
& \frac{\mu_{21}^4 h^4 g(t, y)^3 \left( \frac{d^4}{d(\mu_{21} h) d(\mu_{21}^3 h^3 g(t, y)^3)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right)}{6} +
\end{aligned}$$

$$\frac{\mu_{21}^3 h^3 g(t, y)^2 \left( \frac{d^3}{d(\mu_{21} h) d(\mu_{21}^2 h^2 g(t, y)^2)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right)}{2} + \mu_{21}^2 h^2 g(t, y) \left( \frac{d^2}{d(\mu_{21} h) d(\mu_{21} h g(t, y))} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) + \mu_{21} h \left( \frac{d}{d(\mu_{21} h)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) + \frac{\mu_{21}^4 h^4 g(t, y)^4 \left( \frac{d^4}{d(\mu_{21}^4 h^4 g(t, y)^4)} g(t, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h g(t, y)=0} \right)}{24} + \frac{\mu_{21}^3 h^3 g(t, y)^3 \left( \frac{d^3}{d(\mu_{21}^3 h^3 g(t, y)^3)} g(t, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h g(t, y)=0} \right)}{6} + \frac{\mu_{21}^2 h^2 g(t, y)^2 \left( \frac{d^2}{d(\mu_{21}^2 h^2 g(t, y)^2)} g(t, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h g(t, y)=0} \right)}{2} + \mu_{21} h g(t, y) \left( \frac{d}{d(\mu_{21} h g(t, y))} g(t, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h g(t, y)=0} \right) + g(t, y)$$

(%i6) h[t]=(mu[31]+mu[32])\*h

(%o6) h\_t = (\mu\_{32} + \mu\_{31}) h

(%i7) taylor(h\*(mu[31]\*K[1]+mu[32]\*K[2]),h,0,4)

$$\begin{aligned} & (\%o7) (\mu_{32} + \mu_{31}) g(t, y) h + \left( \mu_{21} \mu_{32} \left( \frac{d}{d(\mu_{21} h)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) + \right. \\ & \left. \mu_{21} \mu_{32} g(t, y) \left( \frac{d}{d(\mu_{21} h g(t, y))} g(t, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h g(t, y)=0} \right) \right) h^2 + \\ & \left( \mu_{21}^2 \mu_{32} \left( \frac{d^2}{d(\mu_{21}^2 h^2)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) + 2 \mu_{21}^2 \mu_{32} g(t, y) \left( \frac{d^2}{d(\mu_{21} h) d(\mu_{21} h g(t, y))} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) \right) h^3 + \\ & \left( \mu_{21}^3 \mu_{32} \left( \frac{d^3}{d(\mu_{21}^3 h^3)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) + 3 \mu_{21}^3 \mu_{32} g(t, y) \left( \frac{d^3}{d(\mu_{21}^2 h^2) d(\mu_{21} h g(t, y))} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) \right) h^4 \end{aligned}$$

(%i8) h[y]=taylorat(%o7)

(%o8) h\_y =

$$\left( \mu_{21}^3 \mu_{32} \left( \frac{d^3}{d(\mu_{21}^3 h^3)} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) + 3 \mu_{21}^3 \mu_{32} g(t, y) \left( \frac{d^3}{d(\mu_{21}^2 h^2) d(\mu_{21} h g(t, y))} g(t + \mu_{21} h, y + \mu_{21} h g(t, y)) \Big|_{\mu_{21} h=0} \right) \right) h^4$$

(%i9) A,%o6,%o8

Maxima encountered a Lisp error:

Error in PROGN [or a callee]: Caught fatal error [memory may be damaged]

Automatically continuing.

To reenable the Lisp debugger set \*debugger-hook\* to nil.

(%i10)